# Language Mod Advanced Smoothing & E

Large Language M[odels: Introduction and](https://tanmoychak.com/) Re

ELL881 · AIL821



Tanmoy Chakraborty Associate Professor, IIT Delhi https://tanmoychak.com/



#### **SearchGPT** announce

OpenAI announces the launch of Sear AI-powered search engine

**SearchGPT** will respond to the questions with up-to-date information from the web while giving links to relevant sources.

#### **SearchGPT●**

Q What are you looking for?

**A new rival to Google and Perplexity?** 

#### Advanced Smoothing Algorithms

- Naïve smoothing algorithms have limited usage and are not very effective. Not frequently used for N-grams.
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	- Kneser-Ney





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- Popular Algorithms:
	- Good-Turing

Use the count of things we've **seen once** to help estimate the count of things we've **never seen**







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Rohan 2

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 $N_1 = 3$ ,  $N_2 = 2$ ,  $N_3 = 1$ 





- You are birdwatching in the Jim Corbett National Park and you have observed the following birds: 10 Flamingos, 3 Kingfishers, 2 Indian Rollers, 1 Woodpecker, 1 Peacock, 1 Crane = 18 birds
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	- Must be less than 1/18





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- Seen once
	- $\bullet$  C = 1
	- MLE  $p = 1/18$

\n- c\* (Woodpecker) = 
$$
2 \times N_2/N_1
$$
\n- =  $2 \times 1/3 = 2/3$
\n- P\*<sub>GT</sub> (Woodpecker) =  $\frac{2}{18}$  = 1/27
\n







## Good Turing Estimation

- Numbers from Church and Gale (1991)
- 22 million words of AP Newswire



Example from Speech and Language Processing book by Daniel Jurafsky and James H. Martin





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It looks like  $c^* = (c - 0.75)$ 



Example from Speech and Language Processing book by Daniel Jurafsky and James H. Martin







#### Absolute Discounting Interpolation

• Adjusts the probability estimates for n-grams by discounting each count by a fixed amount (usually a small constant) before computing probabilities

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P_{\textrm{AbsoluteDiscounting}}(w_i \, | w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c \, (w_{i-1})} + \lambda(w_{i-1}) P(w_i)
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• But considering the regular unigram probability has some limitations, as we will see in the upcoming slides.







- My breakfast is incomplete without a cup of ... : coffee/ Angeles?
- Say, in the corpus "Angeles" more prevalent than "coffee"
- However, it is important to note that "Angeles" mostly comes after "Los"
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- How to compute **continuation probability**?
	- Count how many different bigram types each word completes => Normalize by the total number of word bigram types

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P_{\text{continuation}}(w) = \frac{|\{w_{i-1}: c(w_{i-1},w) > 0\}|}{|\{(w_{j-1},w_j): c(w_{j-1},w_j) > 0\}|}
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#### • **Intuition: Shannon game**

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A common word (Angeles) appearing in only one context (Los) is likely to have a low continuation probability.

#### Kneser-Ney Smoothing

$$
P_{KN}(w_i | w_{i-1}) = \frac{\max(c(w_{i-1}, w_i) - d, 0)}{c(w_{i-1})} + \lambda(w_{i-1}) P_{\text{continuation}}(w_i)
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where,  $\lambda$  is a normalizing constant (How to define this?)







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#### Evaluation of Language Models







### Evaluation of a Language Model

• Does our language model prefer good sentences over bad ones?







#### Evaluation of a Language Model

- Does our language model prefer good sentences over bad ones?
	- Assign higher probability to "real" or "frequently observed" sentences than "ungrammatical" or "rarely observed" sentences
- Terminologies:
	- We optimize the parameters of our model based on data from a **training set**.
	- We assess the model's performance on unseen **test data** that is disjoint from the training data.
	- An evaluation metric provides a measure of the performance of our model on the test set.







#### Extrinsic Evaluation

• Measure the effectiveness of a language model by **testing their performance on different downstream NLP tasks**, such as machine translation, text classification, speech recognition.







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- Measure the effectiveness of a language model by **testing their performance on different downstream NLP tasks**, such as machine translation, text classification, speech recognition.
- Let us consider two different language models: A and B
	- Select a suitable evaluation metric to assess the performance of the language models based on the chosen task.
	- Obtain the evaluation scores for A and B
	- Compare the evaluation scores for A and B







## Intrinsic Evaluation: Perplexity

#### **Intuition: The Shannon Game**

- How well can we predict the next word?
	- I always order pizza with cheese and ...
	- The president of India is ...
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## Intrinsic Evaluation: Perplexity

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	- $\bullet$  I wrote a  $\ldots$
- **Observation:** The more context we consider, the better the prediction.

A better text model is characterized by its ability to assign a higher probability to the correct word in a given context.







The best language model is one that best predicts an unseen test set.

**Perplexity** is the inverse probability of the test data, normalized by the number of words.

• Given a sentence W consisting of *n* words, the perplexity is calculated as follows:

 $PP(W) = P(w_1w_2...w_n)$  $\frac{1}{2}$  $\boldsymbol{n}$ 







Thus, for the sentence W, perplexity is:

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Minimizing perplexity is the same as maximizing probability.

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#### Perplexity and Entropy







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- Large vocabulary leads to high memory requirements.
- High computational cost for large n-grams.
- Lack of generalization to unseen word combinations.





#### The Need for Richer Representations

Requirements:

- **Contextual Understanding:** Need for models that understand context beyond fixed windows.
- **Semantic Similarity**: Ability to capture relationships between words (e.g., synonyms).
- **Scalability:** Models that can scale to large datasets and handle vast vocabularies efficiently.







#### Moving to Word Embeddings & Neural LM

In the successive lectures, we will see how representing words (actually, tokens) as vectors and transition to neural LMs solve many of those problems.







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In the successive lectures, we will see how representing words (actually, tokens) as vectors and transition to neural LMs solve many of those problems.

- Move from discrete to continuous representations.
- Capture richer semantic information.
- Enable generalization to unseen data.
- Scale to large datasets.





### Timeline in Language Modelling







